CONSTRUCTING POVERTY RANKINGS FOR STATE SUBREGIONS: A CASE STUDY OF NORTH CAROLINA

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My own main concern - and, as I perceive it, the concern of the international development community - is with the alleviation of absolute economic misery. Given this judgment, it does not seem desirable to use relative inequality indexes to measure changing income distribution. Rather, it is more appropriate to use absolute income and poverty measures . . . [Fields (1980, p. 182)]

Opposing the use of government to equalize the income distribution is not the same as opposing the use of government to help the poor. It is possible to favor efforts to assist the truly needy while opposing policies that equalize positions among the nonpoor part of the population, and I am far from the first economist (or noneconomist, for that matter) to take this position. [Browning, (1989, p. 826)]

I. Introduction

In recent years, economists with differing views on many income distribution issues have begun to call for a public policy aimed at reducing poverty, rather than income inequality per se. Studies of variations in income inequality among regions have appeared in economics journals for several decades, but less work has been devoted to regional poverty measurement. This paper brings together recent theoretical and statistical advances in poverty measurement and develops a methodology for studying variations in poverty across small regions using readily available data from the Census Bureau.

To illustrate the methodology, we examine subregions of North Carolina, a state with considerable variation in poverty among its major subregions and counties. We find that regional poverty rankings differ substantially from income inequality rankings. Therefore, a public policy which seeks to alleviate absolute economic misery cannot use inequality measures as a guide. Tools specifically designed to identify those regions with the greatest poverty are required.

The measurement of poverty requires that we address three distinct issues. First, any poverty measure necessarily contains ethical judgments about how poverty should be measured. Since our primary objective is to provide ordinal rankings of poverty, we base our study on the judgment that poverty decreases as incomes increase. Second, poverty rankings can be sensitive to the poverty line chosen. We use a methodology suggested by Foster and Shorrocks (1988), which generates poverty rankings using a flexible poverty line. Third, summary measures of poverty (and inequality) are often based on sample data and hence are subject to sampling variability. We address this issue by employing statistical tests for differences in income distributions developed by Beach and Davidson (1983), Bishop (1987), and Bishop, Formby, and Thistle (1989).

The data set for this study is a five percent random sample of North Carolina households from the 1980 Census. Two levels of substate regions can be identified in the data set: the three major subregions (Mountain, Piedmont, and Coastal Plain) of North Carolina, and the Census county groups within the state. The data set does not permit us to identify all counties within the region individually.² The study focuses on the county groups in the Coastal Plain, the poorest of the three major subregions.

The paper proceeds as follows. Section II presents the methodology for generating regional poverty rankings based on sample data. Section III provides the North Carolina regional poverty rankings and contrasts them to rankings based on Gini coefficients and population mean incomes. The final section offers some concluding remarks.

II. Methodology

Poverty Rankings

Dalton (1920), Atkinson (1970, 1987), and others have shown that all inequality and poverty rankings require value judgments. We base our analysis on the judgment that poverty declines if the incomes of the poor increase. Foster and Shorrocks (1988) have shown that this value judgment permits us to generate poverty rankings from truncated order functions. A truncated order function is simply an income vector, $(y_1, y_2, ..., y_N)$, ordered from lowest to highest and truncated at the poverty cut-off. As in comparisons of income inequality with Lorenz curves,

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order functions may cross. Ordinal poverty rankings can only be constructed when the two truncated order functions do not cross below the poverty cut-off.³

This approach, like all attempts to measure poverty, faces the problem that poverty rankings may be sensitive to the location of the poverty cut-off separating the poor and the nonpoor. In particular, contradictory poverty rankings may be obtained when the order function is truncated at different poverty cut-offs. Foster and Shorrocks (1988) propose that we examine a range of poverty lines to check the stability of the rankings. If a poverty ranking is independent of the location of the poverty line within this range, the ranking is considered unambiguous. Otherwise, the poverty comparison is inconclusive.

Figure 1 illustrates several results that play an important role in the approach to poverty measurement used in this paper. First of all, it shows that choosing a poverty income line on the vertical axis is equivalent to limiting the poverty population to some percentage of the total population on the horizontal axis. For instance, if the poverty income line

in Figure 1 is set at C, it follows that the poverty population is limited to the bottom p, percent of the population.

We recognize that the choice of a poverty income line (C) or a poverty population (p_c) is somewhat arbitrary, and that poverty rankings can be sensitive to this choice. However, if we can establish a generous upper bound for the poverty line (or population) and generate identical poverty rankings for alternative poverty lines (or populations) below this upper bound, then the poverty rankings are unambiguous.

Returning to Figure 1, compare the truncated order functions R(X1) and R(X2) for two hypothetical regions. Since R(X1) lies everywhere below R(X2), we can conclude that poverty is more severe in region 1 than in region 2, and justify that conclusion in two ways. First, choose any income on the vertical axis in Figure 1 as the poverty line, and observe that a larger percentage of the population in region 1 has incomes below this poverty line. Alternatively, choose any percentage of the population on the horizontal axis to represent the poor, and observe that the

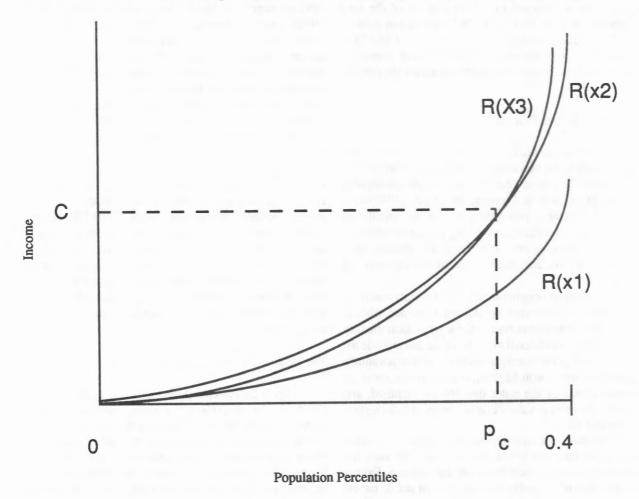


Figure One. Hypothetical Order Functions for Three Income Distributions (X1, X2, and x3)

incomes of the households within this poverty population are smaller in region 1. Provided that R(X1) and R(X2) do not intersect, the relative poverty rankings will remain the same regardless of the location of the poverty cut-off.

Not all comparisons of poverty across regions will be unambiguous, as R(X2) and R(X3) in Figure 1 illustrate. If the poverty income line is set at or below C, the arguments from the previous paragraph can be used to show that poverty is more severe in region 3 than in region 2. However, if the upper bound for the poverty income line is above C, conflicting poverty rankings can be obtained for different poverty lines, and the rankings must be considered ambiguous overall. Thus, Figure 1 shows that unambiguous poverty rankings are possible only when two truncated order functions do not intersect below the upper bound for the poverty cut-off.

In this paper we set an upper bound for the poverty cut-off at the thirtieth percentile in the distribution of households arranged by income. For the United States as a whole, estimates of the size of the poverty population typically range from ten to twenty percent of the total population. For the state of North Carolina, our poverty cut-off translates into a poverty income line of \$8,975 in 1979 dollars. Thus, we believe that the thirtieth percentile of households is a reasonable upper bound for the poverty cut-off.

Statistical Inference Procedures

The empirical analysis in this paper is based on a random sample of households. Meaningful inferences from sample data must take into account the problem of sampling error. Bishop, Formby, and Thistle (1989) have developed statistical procedures to test for significant differences in order functions. Using these procedures to account for sampling error corrects some apparent (i.e., numerical, but not statistically significant) crossings of order functions.

We obtain consistent estimates of the order functions using a vector of conditional (decile) mean incomes. Bishop, Formby, and Thistle demonstrate the asymptotic normality of the vector of conditional mean incomes and provide the variances on which to base equal-means tests. The advantage of this procedure is twofold: first, no assumptions about the parametric form of the order function are required, and secondly, the critical values can be obtained from a standard normal table.

If we accept the null hypothesis of equality at all the decile mean incomes below the poverty line, then the severity of poverty is equivalent in the two regions. Failure to accept the null hypothesis at any pair of decile means requires us to then differentiate between two cases: domi-

nance and noncomparability. We find dominance of region X over region Y if region X has at least one significantly greater decile mean income and no decile mean significantly smaller. We find noncomparability when region X has at least one significantly greater decile mean income and at least one decile mean significantly smaller.

III. Empirical Analysis

To illustrate the methodology described above, we construct poverty rankings for subregions of North Carolina. We divide the state into three major subregions: the Mountains, Piedmont, and Coastal Plain. The poverty rankings for these regions use North Carolina as a whole, the South, and the United States as benchmarks. The Coastal Plain, the poorest of the three major subregions, is then partitioned into 1980 Census county groups. The poverty rankings for the county groups use the Coastal Plain as a whole and North Carolina as benchmarks.

The empirical analysis is based on a five percent random sample of North Carolina households from the 1980 Census of Population and Housing. The basic income measure is Census total household income, which includes wages and salaries, farm and nonfarm self-employment income, interest and dividends, Social Security payments, public assistance payments, and income from several other sources. Households reporting no income are included in the study. Households defined as institutional residences and households with no occupants are not included.

Unfortunately, Census household income does not include taxes or in-kind transfers. A more comprehensive measure of income would be desirable, but the Census has the most complete information readily available for substate regions. Implicitly, we assume that the distribution of taxes and in-kind transfers does not alter the relative poverty orderings based on the Census income definition. Since this paper generates ordinal poverty rankings, rather than cardinal measures of poverty (e.g., headcounts of the poor), the problems created by the Census income measure are not as severe.

The Major Subregions of North Carolina

Figure 2 shows the three major subregions of North Carolina: the Mountains, Piedmont, and Coastal Plain.⁴ Table 1 reports the mean incomes for the bottom three deciles of the major subregions of North Carolina, for North Carolina as a whole, the South, and the United States. Since the mean incomes are based on sample data, standard errors accompany each mean. The poverty income maximum in Table 1 is the highest income contained

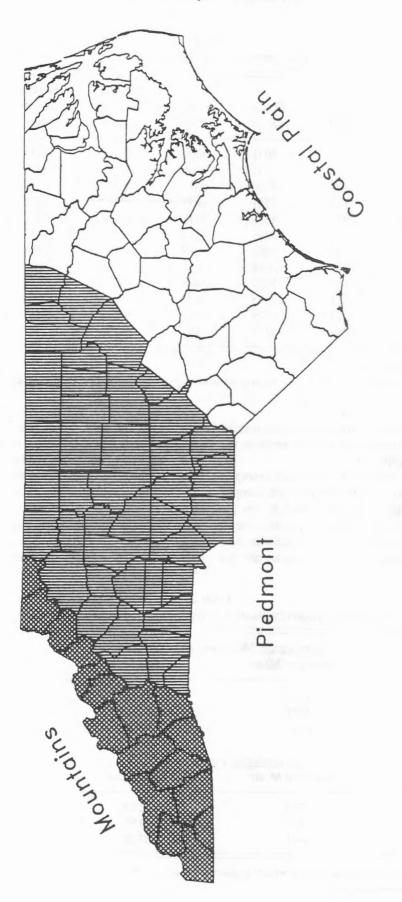


Figure Two. The Major Subregions of North Carolina

Region	First Decile	Second Decile	Third Decile	Poverty Income Maximum	Poverty Income Mean	Sample Size
Coastal Plain	1572	4031	6507	7740	4037	31382
	(32)	(45)	(58)		(131)	
Mountain	1852	4250	6640	7790	4235	10169
	(55)	(78)	(95)		(221)	
North Carolina	1974	4886	7618	8975	4826	104168
	(19)	(29)	(35)		(81)	
South ^b	1893	4963	7989	9510	4948	5174
	(91)	(160)	(204)		(453)	
United States ^b	2149	5354	8478	10005	5327	11696
	(58)	(99)	(115)		(270)	
Piedmont	2273	5529	8440	9900	5414	62617
	(26)	(40)	(48)	(113)		

Table 1

Mean Incomes of the Poor by Region^a

in the third population decile. These figures seem sufficiently high to use the thirtieth income percentile as the upper bound for the poverty cut-off.

Table 2 illustrates the test procedure with examples of poverty dominance and equivalence. In the first example, the mean incomes of the first and second deciles are significantly higher in the Mountains than in the Coastal Plain at the five percent significance level. Within the third decile, the mean incomes of the two regions are not

significantly different. Thus, the Mountains have less poverty overall than the Coastal Plain. Notice that this conclusion would not be altered by relocating the upper bound for the poverty line below the thirtieth percentile.

In the second example in Table 2, there are no significant differences between any of the poverty deciles in the Piedmont and the United States at the five percent significance level. Thus, poverty in the two regions is equivalent. This example underscores the importance of

Table 2
Examples of Inference-Based Poverty Dominance and Equivalence

	Dominance : Mountain	ins and Coastal Plain	
Decile	Mountains Mean	Coast Mean	Test Statistic*
1	1852	1572	4.43
2	4031	4250	2.44
3	6507	6304	0.87
	Equivalence: Pie	edmont and U.S.	
Decile	Piedmont Mean	U.S. Mean	Test Statistic*
1	2273	2149	1.94
2	5529	5354	1.64
3	8441	8478	-0.30

[&]quot;The critical value for the test statistic at the five percent significance level is 1.96.

^{*}Standard errors are in parentheses.

The figures for the South and the United States are based on a random sample of Census households, which is described in detail in Bishop (1987).

Table 3
Pairwise Inference-Based Comparisons of Poverty*

	Coast	Mountains	Piedmont	N Carolina	South	U.S
Coast	aje					
Mountains	+	*				
Piedmont	+	+	*			
North Carolina	+	+	-	*		
South	+	+	-	0	aje	
U.S.	+	+	0	100.+	+	*

*A "+" indicates that the row region has significantly less poverty than the column region (i.e., poverty dominance by the row region).

A "-" indicates the converse. A "0" indicates that the row region and the column region have statistically equivalent poverty (i.e., poverty equivalence).

inference-based poverty rankings. A simple numerical comparison of these regions would lead to the erroneous conclusion that poverty is noncomparable, because the two order functions cross numerically.

Table 3 summarizes the results of all the possible pairwise regional tests. A "+" in Table 3 indicates that the row region has significantly less poverty than the column region. A "-" in Table 3 indicates that the row region has significantly more poverty than the column region. A "0" indicates that poverty in the two regions is statistically

equivalent. For example, the first entry contains a "+" to indicate that there is less poverty in the Mountains than in the Coastal Plain. Similarly, the entry for the United States and the Piedmont is a "0" to indicate the equivalence of the two regions.

It is striking that none of the 15 pairwise comparisons in Table 3 yield a noncomparable outcome. Thus, we are able to construct a complete regional poverty ranking. The Mountains dominate the Coastal Plain, but are dominated by all the other regions. At the other extreme, the United

Table 4County Group Definitions

County Group	Counties Included in Each County Group
Α	Johnston, Lee ^a
В	Nash, Wilson
C	Edgecombe, Halifax, Northampton
D	Beaufort, Bertie, Hertford, Martin, Pitt
E	Camden, Chowan, Currituck, Dare, Gates, Hyde, Pasquotank, Perquimans, Tyrell, Washington
F	Carteret, Craven, Jones, Pamlico
G	Onslow
H	Greene, Wayne
I	Duplin, Lenoir
J	New Hanover
K	Brunswick, Columbus, Pender
L	Bladen, Hoke, Robeson, Scotland
M	Cumberland
N	Harnett, Sampson

Lee county is usually not included in the Coastal Plain, but observations from Johnston and Lee counties cannot be distinquished in the data set. Hence, either Johnston county must be excluded from the definition of the Coastal Plain or Lee county must be included. We chose the latter option.

Table 5
Mean Incomes of the Poor by Census County Group*

County Group	First Decile	Second Decile	Third Decile	Poverty Income Maximum	Poverty Income Mean	Sample Size	
A	1709	4090	6581	7805	4126	1890	
	(138)	(171)	(244)		(532)		
В	1800	4389	7107	8300	4432	2261	
	(109)	(191)	(219)		(511)		
C	1243	3380	5363	6505	3329	2195	
	(122)	(128)	(195)		(426)		
D	1262	3364	5612	6865	3413	3377	
	(96)	(110)	(216)		(517)		
E	1617	4069	6627	7755	4104	1991	
	(122)	(190)	(216)		(517)		
F	1709	4223	6868	7965	4267	2274	
	(106)	(195)	(194)		(490)		
G	2049	5471	7381	8370	4967	1521	
	(186)	(207)	(199)		(580)		
H	1826	4327	6667	8005	4273	1881	
	(121)	(175)	(248)		(532)		
I	1524	3684	6018	7170	3742	1741	
	(135)	(178)	(225)		(515)		
J	1939	4602	7282	8700	4608	1896	
	(134)	(195)	(269)		(584)		
K	1403	3406	5798	7040	3536	1855	
	(121)	(156)	(243)		(502)		
L	1574	3766	6138	7260	3826	2892	
	(92)	(141)	(173)		(398)		
M	1437	4265	6616	7735	4106	1548	
	(136)	(236)	(226)		(588)		
N	1923	5633	8340	9580	5299	2212	
	(161)	(224)	(219)		(593)		

^{*}Standard errors are in parentheses.

States and the Piedmont dominate all other regions. Also, poverty in North Carolina as a whole is equivalent to poverty in the South.

The Census County Groups in the Coastal Plain

The significant differences in poverty among the major subregions of North Carolina lead us to consider variations in poverty among the Census county groups. We focus on the county groups in the poorest of the three regions, the Coastal Plain. To facilitate exposition, the county groups in the Coastal Plain are assigned the letters A through N (see Table 4). Table 5 provides the mean incomes and standard errors for the poverty deciles in these fourteen county groups.

The point estimates themselves would suggest numerous instances (e.g., L and M) in which the poverty comparisons are inconclusive due to sensitivity to the location of the poverty line. However, statistical tests at the five percent significance level eliminate any ambiguity in the 91 pairwise comparisons. Thus, the poverty rankings do not depend on the location of the poverty line within the bottom three deciles. This result allows us to summarize the poverty rankings using the cumulative mean incomes of the three poverty deciles.

Table 6 ranks the county groups in the Coastal Plain from lowest to highest by the mean income of the poor, by a Gini index of equality, and by the mean income of the total population. Each column in Table 6 is normalized by setting the mean for North Carolina to 1.00. A single

	(2)		(4)		(6) Population
County		County	Income	County	Mean
Group	Poverty ^a	Group	Equality ^b	Group	Incomec
С	.68	D	.934	N	.81
D	.71	C	.941	L	.85
K	.73	K	.945	C	.85
		- I	.958	I	.86
I	.78**			- K	.86
L	.79**	Coast	.976		
N	.80**	A	.978**	G	.88**
Coast	.83	J	.979**	D	.88**
E	.84**			- E	.89**
Α	.85**	В	.982*	Mountains	.89**
		- F	.982*	Coast	.90
Mountains	.88	L	.983*	H	.91**
F	.88	Mountains	.992*	A	.92**
H.	.88	H	.992*		
В	.91	N	.992*	F	.93
J	.95*	E	.994*	M	.95
N Carolina	1.00	N Carolina	1.000	В	.97*
G	1.05*	Piedmont	1.018*	N Carolina	1.00
M	1.11	G	1.037	J	1.05
Piedmont	1.12	M	1.058	Piedmont	1.10

Table 6
Comparison of Poverty, Income Equality, and Mean Income Rankings

asterisk indicates that a county group is not significantly different from the state. Two asterisks indicate that a county group is not significantly different from the Coastal Plain. The dashed lines in Table 6 separate the county groups in each column into three categories: below average for the Coastal Plain, average for the Coastal Plain, and above average for the Coastal Plain.

Figure 3 maps the county groups in the Coastal Plain according to these three categories. The map illustrates the heterogeneity of the Coastal Plain and identifies two subregions with poverty rankings significantly below average for the Coastal Plain. A public policy aimed specifically at reducing poverty (as opposed to inequality <u>per se</u>) would have to focus on these pockets of poverty.

The results in Table 6 provide evidence that neither the Gini equality rankings nor the population mean income rankings are good substitutes for poverty rankings. Consider county group N for example, which has a poverty ranking equivalent to the Coastal Plain, but significantly more equal incomes and a significantly lower population mean income. Consider county group G as well, which has a poverty ranking equivalent to the state, but significantly more equal incomes and a significantly lower population mean income. County group J has a significantly greater population mean income and significantly less equal incomes than the State, but an equivalent poverty ranking. Along with other comparisons that could be pointed out from Table 6, these findings suggest that neither the Gini

^{*}Equivalent to North Carolina at the 5 percent significance level.

^{**}Equivalent to the Coastal Plain at the 5 percent significance level.

[&]quot;The measure of poverty is PovMean(X)/PovMean(NC), where PovMean(X) is the cumulative mean income of the poor for any county group X and PovMean(NC) is the cumulative mean income of the poor for North Carolina (\$4826).

The measure of income equality is [1 - Gini(X)]/[1 - Gini(NC)], where Gini(X) is the Gini coefficient for any county group X and Gini(NC) is the Gini coefficient for North Carolina (0.391).

[&]quot;The measure of population mean income is Mean(X)/Mean(NC), where Mean(X) is the population mean income for any county group X and Mean(NC) is the population mean income for North Carolina (\$16,479).

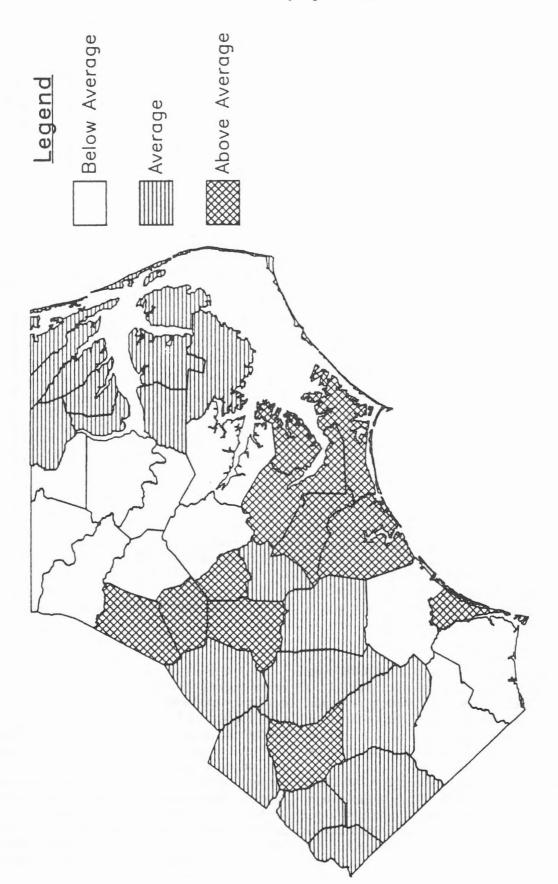


Figure Three. The Coastal Plain

Mean Incomes of the Poor Relative to the Coastal Plain

equality rankings nor the population mean income rankings provide satisfactory substitutes for poverty rankings.

IV. Conclusions

We present a methodology for studying variations in poverty across small regions using readily available data from the Census Bureau. This methodology checks for ambiguity in poverty rankings due to variations in the location of the poverty line. The regional poverty rankings obtained here are not sensitive to the location of the poverty line within a reasonable range. This conclusion is based on recently developed statistical inference procedures which test for significant differences in poverty rankings among regions.

The methodology is applied to major state subregions and Census county groups in North Carolina, which shows considerable variations in poverty among its regions. The regional poverty rankings for North Carolina are compared to rankings by income equality and population mean incomes. We find important differences among these rankings. This finding suggests that a public policy that seeks to alleviate absolute economic misery cannot use inequality measures as a guide. Instead, tools specifically designed to identify regions with the greatest poverty are required.

Notes

¹Recent extensions of this line of research include Amos (1986) and Maxwell and Peter (1988), which contain references to the previous literature.

²In sparsely populated regions, as parts of the Coastal Plain are, the Census Bureau does not identify counties individually in public use microdata to ensure the anonymity of household records.

³Of course, with stronger value judgments, unambiguous poverty comparisons can be obtained. However, stronger value judgments will command less general agreement.

The boundaries for the major subregions are taken from Clay,

Orr, and Stuart (1975). The only exception is Lee county, which is included in the Coastal Plain because the Census data combines it with Johnston county.

⁵Formulas for the lower-bound Gini coefficients and their variances are given by Beach and Davidson (1983).

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