APPLICATION OF COUNT DATA PROCEDURES TO ESTIMATE THRESHOLDS FOR RURAL COMMERCIAL SECTORS

Thomas R. Harris, Kalyan Chakraborty, Lijuan Xiao, and Rangesan Narayanan*

Abstract-This paper extends previous research in the estimation of minimum demand thresholds for rural commercial sectors by employing count data procedures. Advantages of count data procedures are contrasted with the traditional double-log model. Also discussed is the incorporation of results from count data procedures into a rural commercial sector development strategy.

I. INTRODUCTION

Traditionally, rural economic development has concentrated on the recruitment and attraction of export-oriented, goods-producing industries. Industrial recruitment yields industries which are primarily export-oriented and provide a base for existing local economic sectors while generating input demands for further economic development. Important for local economic development professionals, attraction of a goods-producing industry such as manufacturing is highly visible. The direct employment and income effects of the relocated industry are measurable and the local community economic development team usually reaps abundant media coverage.

Nonetheless, industrial recruitment programs prove to be costly, risky and often yield little payoff. Rural communities are often unsuccessful at industrial recruitment because these communities have very limited resources (Hansen 1970). In order to attract goods-producing industries, rural communities with meager resources often grant tax concessions to new or relocating firms, thereby eliminating opportunities for fiscal gain (Kieschnick 1981, Shaffer 1989). Usually the outcome of this type of industrial recruitment is that the local tax burden of the resident populace in the local community increases because increased community

^{*}Thomas R. Harris is a Professor in the Department of Agricultural Economics and Director of the University Center for Economic Development at the University of Nevada, Reno. Kalyan Chakraborty is a former Graduate Research Associate in the Department of Agricultural Economics. Lijuan Xiao is a former Graduate Student in the Department of Agricultural Economics. Rangesan Narayanan is Professor and Chair in the Department of Agricultural Economics at the University of Nevada, Reno. The authors would like to express gratitude to J.S. Shonkwiler for review of this article. This research was conducted under funding by the Nevada Agricultural Experiment Station Project No. 219 and the University Center for Economic Development.

services for the new industry are incurred without an expanding tax base due to the tax moratoria (Tweeten and Brinkman 1976). Moreover, firms willing to relocate because of incentives and tax abatements are also likely to leave the community if other communities offer better inducements. Results of recent surveys (Smith and Fox 1990; McNamara and Kriesel 1993) continue to show that planning commissions still emphasize the recruitment of export-oriented or goodsproducing industries, while the pursuit of alternative economic development strategies, such as local services and retail sector development, are largely overlooked and often neglected.

Questions regarding the development and expansion of rural commercial sectors may be addressed by the economic development strategy of import substitution. Import substitution seeks to replace goods and services imported from outside the area with local sources of supply (Shaffer 1989). Because expenditures remain inside the local economy instead of being lost to imports, import substitution strategies strengthen linkages within the local economy. Also, keeping earned surplus within the local economy enhances local employment and incomes (Smith, 1994). For current and future time periods, local economic development strategies must give balanced emphasis to the formulation of import substitution strategies as well as relocation of goods-producing industries.

A commercial sector market analysis tool commonly used to estimate rural commercial sector activity is demand threshold analysis. The demand threshold is defined as the minimum market size required to support a particular good or service and still yield an acceptable rate of return for the business owner (Berry and Garrison 1958a, 1958b; Parr and Denike 1970); Salyards and Leitner 1981 and King 1984). The concept is based on the internal economy of the firm and the characteristics of consumer demand. As dictated by central place theory, (the foundation for threshold analysis), thresholds are not absolute, but vary by good and service. Demand thresholds are usually measured in terms of population required to support one or more firms of a certain type.

Empirical estimates of market thresholds are numerous (Berry and Garrison 1958a, 1958b; Foust and Pickett 1974; Murray and Harris 1978; Salyards and Leitner 1981). However, all of the past studies employed ordinary least squares procedures and truncated data sets, which may provide biased estimates. This paper examines the use of count data procedures to estimate threshold levels for rural retail establishments. Specific objectives are to review demand threshold analysis, to discuss count data procedures, and review threshold demand results employing count data procedures.

A Review of Market Threshold Analysis

Threshold analysis is rooted in central place theory (CPT) in two ways. First, CPT predicts that there is a direct and positive relationship between the population of the central place and the number of firms. Here, number of functions can be proxied by the number of firms within the central place. In other words, as the population of the central place increases, so do the number of firms within the place.

Second, and perhaps more fundamental, CPT predicts that goods will have a specific limitation to the size of their market in a spatial sense. The radius of this market determines the range of the good. The larger the range of the good, the larger the spatial size of the market supporting that good. The key determinants of a good's range are the demand for the good and the cost of supplying the good. Specifically, the interaction of the Losch demand cone and the firm's average cost curve determines the range or market size of the good. Given that the cost structure facing the firm is determined exogenously from CPT (i.e., factor prices and good's production technology) the primary determinant of a good's range, or spatial market, will be the characteristics of the good's aggregate demand structure (i.e., demand cone). A spatial equilibrium is achieved when the dollar volume under the demand structure is just sufficient to cover operating costs and allow an acceptable rate of return.

Threshold analysis attempts to proxy the demand structure for a good by relating population to the number of functions (i.e., number of businesses) within a particular central place. Berry and Garrison (1958a, 1958b) suggested that this relationship can be expressed as

$$P = \alpha B^{\beta} \tag{1}$$

where P is the place's population, B is the number of businesses of a particular type within the place, and α and β are parameters to be estimated. The nonlinear specification follows from CPT. In practice, the estimated equation is a double-log model. Given estimates of α and β , one may substitute B = 1 and solve for the population required to support one firm. Hence, a proxy measure for the size of the supporting demand structure for the good is provided.

The use of this specification for estimating market thresholds raises several problems. First, the use of a logarithmic transformation affects the nature of the estimates produced. The regression procedures estimate the logarithm of the number of businesses, not the number of businesses themselves. The antilog of these estimates are biased estimates of the number of businesses (Haworth and Vincent 1979).

A second difficulty arises by the use of the logarithmic transformation when a place's number of businesses for a particular type is zero. Since the logarithm of zero is negative infinity, a small positive number is usually added to all observations, or zero observations are removed from the sample. In rural areas where there are numerous places with no retail activity in some sectors, this difficulty can lead to serious problems. Adding a small positive number will result in upward, nonparallel shift of the relationship and biased estimates of threshold populations.

A third problem many past researchers seemed to share was a reversal of the logical cause-effect relationship between population and number of businesses (Chrisman 1985). Berry and Garrison (1958a) for example, regress number of businesses onto population. Because the number of businesses is the random variable within the problem, placing it on the right-hand side of the equation results in both biased and inconsistent estimates. Not all threshold studies, however, are subject to this shortcoming (Foust and de Souza 1977; Foust and Pickett 1974).

A fourth shortcoming of the bulk of the empirical threshold literature is the sparseness of the specification of the estimated equation. Numerous studies use population as the sole determinant of market demand. As argued by Murray and Harris (1978), the number of businesses supported by a given population is influenced by many factors. Other studies or retail activity have determined that socioeconomic factors, such as income levels and distribution, population density and spatial competition, can dramatically affect the size and shape of the market demand cone (Deller and Chicoine 1989; Henderson 1990). By omitting relevant variables, the parameter estimates will be biased.

A final problem concerns the use of OLS procedures to estimate numbers of businesses. Ordinary least squares assume that the number of businesses are normally distributed, which implies that the possible values which can be taken by the random variable are normally distributed around the estimate. There is little reason to suppose the values are normal. In fact, the number of firms is a nonnegative integer which would suggest count data procedures.

Count Data Procedures

Count data procedures can be used when the dependent variable takes on values that are only non-negative integer values corresponding to the number of events (or number of stores) occurring in a given interval (or community). In such cases, the Poisson regression model has been used to analyze count data. The model stipulates that each Y_i is drawn from a Poisson distribution with parameter λ_i , which can be parameterized to depend upon the regressors, X_i 's. The Poisson distribution is stated as:

$$Prob(Y_i = y_i) = \exp(-\lambda_i) \frac{\lambda_i^{y_i}}{y_i!} \qquad y_i = 0, 1, 2, ...$$
(2)

The most common formulation for λ_i is to assume λ_i is loglinearly dependent on explanatory variables or:

$$\ln \lambda_{i} = \beta_{0} + \sum_{j=1}^{P} \beta_{j} X_{ij}$$
(3)

$$i = 1, 2, ..., n$$

$$j = 1, 2, ..., P$$

The Poisson distribution is simply a nonlinear regression. Estimation of parameters is made through maximum likelihood techniques or the log-likelihood function which is:

$$lnL = \sum_{i=1}^{n} -\lambda_{i} + \beta_{0} \sum_{i+1}^{n} Y_{i} + \sum_{j=1}^{P} \beta_{j} \sum_{i=1}^{n} X_{i} Y_{i} - \sum_{i=1}^{n} ln(Y_{i} !)$$
(4)

The Poisson distribution was estimated using the LIMDEP package of Greene (1989).

Several studies have been completed using the Poisson regression model in econometric and statistical literature. Advances in the theory of estimation can be found in works by Jorgenson (1961); Frome, et al. (1973); Gourierox et al. (1984); Terza (1985); and Madala (1983). The technique has been successfully applied by Flowerdew and Aitkin (1982); Hausman et al. (1984); Gilbert (1979) and Cameron et al. (1984). An excellent literature review and general overview of count data modeling is presented in a referenced study by Cameron and Trivedi (1986).

However, when using a Poisson distribution for count data analysis, it is assumed that the conditional mean of the dependent variable, λ_i is equal to the conditional variance; i.e., the variance-mean ratio is one. Overdispersion of the population is defined as the conditional variance of the dependent variable exceeding its conditional mean, giving a variance-mean ratio greater than one. Overdispersion is a form of heteroscedasticity. If the population is overdispersed, the Poisson model will yield consistent estimates of the parameters but downwardly biased estimates of the standard errors (Gourieroux et al. 1984). The generalization of the Poisson distribution, which is often used to model such counts, is the negative binomial distribution (Hausman et al. 1984; Cameron and Trivedi (1986). The negative binomial distribution is an extension of the Poisson distribution which allows the variance of the process to differ from the mean. The negative binomial arises from the Poisson model by specifying:

$$\ln \lambda_i = \beta X + \epsilon, \tag{5}$$

where \in has a gamma distribution with mean parameter Φ and index (or precision) parameter α_i . The mean and variance of the negative binomial distribution are given by:

$$E[Y_i] = \Phi_i \tag{6}$$

$$Var[Y_i] = \Phi_i + \frac{1}{\alpha_i} \Phi_i^2$$
(7)

Since $\Phi_i > 0$ and $\alpha_i > 0$, it is clear that the variance exceeds the mean, so the model allows for overdispersion. Using the LIMDEP software, maximum likelihood estimates for the negative binomial are obtained. Starting values are obtained from Poisson parameters and an estimate of the variance of Y_i .

Model Specification

Not all states have sales taxes, but for those states that have a sales tax, retail sales may not be recorded at point of sale. The eight two-digit SIC retail sectors from the 1987 Census of Retail Trade (1990) were used to derive minimum demand thresholds. ¹ Data for the minimum demand analysis were gathered from the 1988 *City and County Data Book* (1988) and the 1987 *Census of Retail Trade* (1990). The final data set contained 2,126 communities. This study differs from most other market threshold studies because the unit of observation is the county as opposed to town or city. It would have been advantageous to complete the analysis at the community level; however, for some states the only reliable retail establishment numbers are produced at the county level by the Census of Retail Trade. ² Therefore it is anticipated that the market population estimates from this study may not be directly comparable to previous studies.

For this analysis, the double log, Poisson, and negative binomial models were employed where:

B = f(POP, PCI, PPBEL, DEN, UNRATE, PESTiiS, ADJ)(8) where:

B is the number of retail establishments by type

POP is population in 1986

PCI is per capita income in 1985

PPBEL is the percent of persons below poverty level (1979)

DEN is the population density (1986)

UNRATE is the unemployment rate (1986)

- PESTiiS is the percent of total number of establishments in SICii that are small (defined as having no employees)
- ADJ is the dummy variable for adjacency to metropolitan counties (1 = yes; 0 = no)

For this analysis, population, per capita income, and population density were transformed into log values. The inclusion of explanatory variables beyond population builds upon the models developed by Murray and Harris (1978). Per capita income, percent of persons below poverty level, and unemployment rate were intended to capture the buying power of consumers within a county. It is expected that per capita income will be positively related to number of firms because of enhanced buying power by local residents, while increases in poverty level and unemployment rate would be negatively related. Population density was a proxy for ruralness of a retail market and is expected to be positively related. The metropolitan adjacency dummy captures the spatial competition and is expected to be negatively related due to heightened spatial competition of metropolitan retailers.

Inclusion of the percentage of businesses that are deemed small-that is, having no employees-is designated to capture the mix of retail businesses within a particular sector. Previous market threshold studies have implicitly assumed that businesses within a retail sector have identical cost structures. However, in rural retail markets, this may be false. For example, one county of a certain size may have one large retail store, while another county of similar population size has four small retail stores supporting local demand. Specifically, one retail market will appear to be under-retailed while the other would be classified as over-retailed. Inclusion of this variable attempts to address this problem and is assumed to be positively related to the number of retail establishments.³

Results

Table 1 shows the results of the negative binomial procedures where population, per capita income, and population density were expressed in logarithmic form for the eight two-digit retail SIC sectors. Of interest is the coefficient for the negative binomial that had significant t-values for all eight retail sectors. This in-

wimmum	Demand	These	Iolu Estil	mates Us	sing racg	ative Dinoi	IIIai FIOC	equies
Variable	SIC-52	SIC-53	SIC-54	SIC-55	SIC-56	SIC 57	SIC 58	SIC 59
Intercept	-6.2931	-6.4079	-10.0290	-6.4053	-22.368	-14.5140	-9.5857	-12.9030
	(9.83) ^b	(7.50)	(18.66)	(12.94)	(30.98)	(21.92) ^b	(18.94)	(28.65)
Population ^a	0.8908	0.8593	0.8799	0.9409	1.1294	1.0619	1.0384	0.9983
	(71.78)	(53.86)	(82.67)	(88.45)	(63.03)	(78.03)	(75.74)	(96.92)
Per Capita								
Income ^a	0.0839	-0.0378	0.5306	0.0751	1.5203	0.7464	0.4397	0.8440
	(1.20)	(0.41)	(8.52)	(1.42)	(20.29)	(10.64)	(8.33)	(18.00)
% Below								
Poverty	-0.0112	0.0119	0.0255	-0.0031	0.0197	0.0007	-0.0216	-0.0058
	(6.41)	(5.45)	(16.51)	(2.31)	(8.92)	(0.39)	(14.20)	(4.13)
Population								
Density ^a	-0.0786	-0.0051	0.0169	-0.0294	-0.0469	0.0189	-0.1739	-0.0869
	(8.61)	(0.43)	(2.10)	(3.52)	(3.80)	(2.05)	(16.57)	(11.52)
Unemployment								
Rate	-0.0178	-0.0038	0.0055	-0.0046	-0.0046	-0.0152	-0.0029	-0.0070
	(9.36)	(1.56)	(3.33)	(2.84)	(1.97)	(7.09)	(1.56)	(5.30)
% Small								
Establishments	-0.0008	0.0045	0.0080	0.0091	0.0024	0.0023	0.0036	0.0027
	(1.78)	(10.07)	(16.32)	(23.95)	(7.84)	(6.43)	(6.78)	(5.48)
Adjacent								
Dummy								
Variable	-0.0667	-0.0816	-0.0578	-0.0835	-0.3396	-0.2223	-0.1179	-0.1278
	(4.48)	(4.63)	(4.41)	(7.11)	(16.40)	(13.83)	(7.17)	(9.81)
	0.0320	0.0293	0.0456	0.0352	0.1082	0.0430	0.0968	0.0571
α	(11.55)	(7.97)	(21.62)	(23.91)	(21.77)	(16.02)	(30.88)	(35.39)

TABLE 1

Minimum Demand Threshold Estimates Using Negative Binomial Procedure

^a Values are in log

^b Absolute values of the t-statistic in parenthesis

dicates that overdispersion exists and that the negative binomial results should be employed for the count data analysis.⁴

The performance of the individual variables is in general as expected. By far the most dominant variable, as suggested by theory and previous empirical work, was population. In each case population was positive as expected and significant. Also, where significant, per capita income is positive. For most retail sectors, the number of establishments tends to be more sensitive to changes in population than changes in per capita income. This result is consistent with a previous study by Henderson (1990). Performance of the remaining independent variables was mostly consistent with prior expectations. Also, the variable accounting for variation in establishment size mix, when significant, had the correct sign. For all eight retail sectors, counties adjacent to a metropolitan area tend to support fewer establishments, given all other variables held constant.

In Table 2, the population thresholds are reported for a given number of firms by retail SIC. Due to the inclusion of several socio-economic variables within the specification of the threshold equations, market population estimates can be uniquely derived for any given county. For illustrative purposes, assume

	Number of Firms						
SIC	1	2	3	4	5		
52 Building/ Gardening Merchandise	1,060	2,309	3,640	5,027	6,458		
53 General Merchandise	1,399	3,045	4,801	6,631	8,518		
54 Food Store	151	332	527	731	942		
55 Automobile Dealers and Gasoline Stations	378	791	1,216	1,651	2,093		
56 Apparel and Accessory Stores	1,894	3,498	5,009	6,463	7,874		
57 Furniture and Home Furnishings	1,507	2,894	4,240	5,559	6,859		
58 Eating and Drinking Places	555	1,082	1,598	2,109	2,614		
59 Miscellaneous Retail	285	570	856	1,142	1,427		

TABLE 2 Population Required to Support a Given Number of Firms by SIC Class Based on Negative Binomial Estimates.

that the analyst is interested in market population for an average non-adjacent county (Table 3). For Apparel and Accessory Stores, using negative binomial procedures, the minimum demand for one store is 1,894; for two it is 3,498; for three it is 5,009; for four it is 6,463, and for five it is 7,874 for average values of nonadjacent rural counties. If ordinary least squares procedures are employed, the minimum demand for one store is 2,109; for two it is 3,831; for three it is 5,433; for four it is 6,960 and for five it is 8,435. The calculated minimum demand threshold for the above example is lower when negative binomial procedures are employed. One reason is that the negative binomial does not truncate the data, but allows zero values to be incorporated in the estimation procedures. Also, because the number of retail establishments is not normally distributed, the analysis should be applied with count data procedures such as the negative binomial.

In addition, another application of negative binomial procedures is that the expected number of retail establishments for a given county can be estimated. For the average non-adjacent nonmetropolitan county, the expected number of apparel and accessory stores is 15.03. When the expected value is compared to actual establishment numbers, economic development professionals can use this information to pursue retail development strategies. In addition, count data procedures

Variables	Units	Value	
Population	nos.	20,861	
Per Capita Income	\$	7,805	
Percent Below Poverty	%	17.73	
Population Density	nos.	32.09	
Unemployment Rate	%	9.30	
Percent Small Establishments for SIC 52	%	34.38	
Percent Small Establishments for SIC 53	%	30.35	
Percent Small Establishments for SIC 54	%	36.94	
Percent Small Establishments for SIC 55	%	38.11	
Percent Small Establishments for SIC 56	%	31.56	
Percent Small Establishments for SIC 57	%	51.04	
Percent Small Establishments for SIC 58	%	26.83	
Percent Small Establishments for SIC 59	%	61.55	

TABLE 3 Independent Variable Values for an Average Non-Adjacent County

such as the negative binomial can derive the probability of a given number of apparel and accessory stores existing in an average nonadjacent nonmetropolitan county. For the apparel and accessory store example, the probability of no apparel and accessory stores is 0 percent, while for 13 stores it is 9.52 percent; for 14 stores it is 10.22 percent; for 15 stores it is 10.24 percent and for 16 stores it is 9.62 percent. Using the highest probability value, the example county has a threshold for 15 stores which correspond to the expected value.

Results from ordinary least squares procedures would produce minimum threshold values but could not estimate probabilities of a given number of establishments. The probability results from the negative binomial could be incorporated into a retail development strategy. This would give economic development professionals an estimate of potential risks in advocating a given retail development strategy. Past retail development strategies which employ minimum demand thresholds derived from ordinary least squares procedures have been unable to incorporate risk into a development plan.

Conclusions

The primary objective of this paper was to add upon previous minimum demand threshold studies in two regards. First, contemporary minimum demand threshold studies built around population have several disadvantages ranging from model misspecification to unnecessary structure due to a specific functional form. Second, an alternative approach to ordinary least squares procedures was applied

to estimate minimum thresholds. Because retail store establishment numbers are non-negative and integer values, the assumption that retail business counts are normally distributed is suspect. Business establishment numbers are characterized as count data where the Poisson and negative binomial distribution are better suited. Results from the negative binomial distribution indicated that the number of retail establishments were overdispersed, so the negative binomial was the appropriate procedure to employ in estimating minimum thresholds.

Following suggestions by Murray and Harris, (1978) additional socioeconomic data besides population was used to derive minimum thresholds. Results indicated that county population and per capita income, when significant, were positive influences on the number of retail establishments. Also, results indicated that number of retail establishments were more sensitive to population change than per capita income. In addition, for all retail sectors analyzed, counties adjacent to a metropolitan county tend to support fewer establishments, given all other variables held constant.

Previous market threshold studies have not addressed the probability of the number of retail establishments, given socio-economic characteristics of a county. Results of the negative binomial can derive probabilities of a given number of retail firms existing in a given county. Through the use of count data procedures, economic development strategies can incorporate risk of promotion of retail development in their county economy.

ENDNOTES

1. The eight retail sectors employed in this analysis were Building Materials and Garden Supply Stores (SIC 52); General Merchandise Stores (SIC 53); Food Stores (SIC 54); Automotive Dealers and Gasoline Service Stations (SIC 55); Apparel and Accessory Stores (SIC 56); Furniture and Home Furnishing Stores (SIC 57); Eating and Drinking Establishments (SIC 58) and Miscellaneous Retail Establishments (SIC 59).

2. In some states, sales taxes are not collected, and where sales taxes are collected, retail sales may be recorded at regional or state headquarters rather than at point of sale. Therefore Census of Retail Trade establishment numbers were used because of reliability of establishment numbers. Of course, where available, community retail establishment numbers are preferred.

3. Minimum demand threshold models tend to be demand driven, assuming identical cost structures across commodity groups. One possible source of misspecification is the omission of supply-related factors, specifically operating costs, which will affect returns.

4. Minimum thresholds were derived for ordinary least squares and Poisson procedures. Because of space limitations results of these procedures are not presented.

REFERENCES

- Berry, B., and W. Garrison. "A Note on Central Place Theory and the Range of Good." *Economic Geography*, 34 (1958a): 304-311.
- Berry, B., and W. Garrison. "Recent Developments in Central Place Theory." Proceedings of the Regional Science Association. 4(1958b): 107-121.
- Cameron, A., and P. Trivedi. "Econometric Models Based on Count Data: Comparisons and Applications of Source Estimators and Tests." *Journal of Applied Econometrics*, 1(1986): 29-53.
- Cameron, A., P. Trivedi, F. Milne and J. Piggot. "Microeconomic Models of the Demand for Health Insurance and Health Care in Australia: II." Working Papers in Economics and Econometrics No. 106, Australian National University, 1984.
- Chrisman, J.J. "Population Change and Its Effect on the Retail Sector: An Exploratory Study," *International Small Business Journal*, 3 (1985):26-46.
- Deller, S.C., and D.L. Chicoine. "Economic Diversification and the Rural Economy: Evidence from Consumer Behavior," *Regional Science Perspectives* 19 (1989):41-55.
- Flowerdew, R., and M. Aitkin. "A Method of Fitting the Gravity Model Based on the Poisson Distribution." *Journal of Regional Science*, 22(1982): 191-202.
- Foust, B., and A. DeSouza. The Wisconsin Urban System: Functional Size, Trade Area and Nesting. Unpublished manuscript, Department of Geography, University of Wisconsin, Eau Claire, 1977.
- Foust, B., and E. Pickett. Threshold Estimates: A Tool for Small Business Planning in Wisconsin. Unpublished manuscript, Department of Geography, University of Wisconsin, Eau Claire, 1974.
- Frome, E., M. Kutner and J. Beauchamp. "Regression Analysis of Poisson-Distributed Data." Journal of the American Statistical Association. 68(1973): 935-940.
- Gilbert, C. "Econometric Models for Discrete Economic Processes." *Discussion Paper*, University of Oxford, Presented at the Econometric Society European Meeting, Athens, 1979.
- Gourieroux, C., A. Monfort and A. Trognon. "Pseudo Maximum Likelihood Methods: Applications to Poisson Models." *Econometrica*. 52(1984):701-720.

- Green, W. LIMDEP: User's Manual. New York: Econometric Software, Inc., 1989.
- Hausman, J. B. Hall and Z. Griliches. "Econometric Models for Count Data with an Application to Patents-R&D Relationship. *Econometrica*, 52(1984): 909-938.
- Hansen, N. Rural Poverty and the Urban Crisis. Bloomington, Indiana: Indiana University, 1970.
- Haworth, J., and P. Vincent. "The Stochastic Disturbance Specification and Its Implications for Log-Linear Regression." *Environment and Planning A*, II(1979):781-790.
- Henderson, D. "Retail Sales and Consumer Expenditure Functions." Journal of Agricultural Research, 42(1990):27-34.
- Jorgenson, D. "Multiple Regression Analysis of a Poisson Process." Journal of the American Statistical Association. 56(1961): 235-245.
- Kieschnick, M. Taxes and Growth: Business Incentives and Economic Development. Washington, D.C.: Corporation for Enterprise Development, 1981.
- King, L.J. Central Place Theory. London: SAGE Publications, 1984.
- Madala, G. Limited-Dependent and Qualitative Variables in Econometrics. New York: Cambridge University Press, Economic Society Monographs No. 3, 1983.
- McNamara, K., and W. Krissel. "Assessing Local Industrial Development Potential." Journal of the Community Development Society, 24(1993):61-71.
- Murray, J. and J. Harris. A Regional Economic Analysis of the Turtle Mountain Indian Reservation: Determining Potential for Commercial Development. Prepared for the Federal Reserve Bank of Minneapolis, Minneapolis, Minnesota, 1978.
- Parr, J., and K. Denike. "Theoretical Problems in Central Place Analysis." Economic Geography, 47(1970): 568-586.
- Salyards, D.M., and K.R. Leitner. "Market Threshold Estimates: A Tool for Business Consulting in Minnesota." American Journal of Small Business, 6(1981): 26-32.
- Shaffer, R. Community Economics: Economic Structure and Change in Small Communities. Ames, Iowa: The Iowa State Press, 1989.
- Smith, D. "Native American Economic Development: A Modern Approach." The Review of Regional Studies, 24(1994):87-102.
- Smith, T., and W. Fox. "Economic Development Programs for States in the 1990's." *Economic Review*, July/August (1990):25-35.
- Terza, J. "A Tobit-Type Estimator for the Censored Poisson Regression Model." Economic Letters, 18(1985):361-365.

- Tweeten, L., and G. Brinkman. Micropolitan Development: Theory and Practice of Greater Rural Economic Development. Ames, Iowa: The Iowa State Press, 1976.
- U.S. Department of Commerce. 1987 Census of Retail Trade: Geographic Area Series. Washington, D.C. Bureau of the Census, 1990.
- U.S. Department of Commerce. *County and City Data Book*. Washington, D.C. Bureau of the Census, 1988.
- Xiao, Lijuan. "Estimation of Thresholds for Rural Commercial Sectors: Application of Count Data Procedures." Unpublished Master's Thesis, Department of Agricultural Economics, University of Nevada, Reno.